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Artificial Intelligence Techniques for Enhancing Thermo-Electro-Mechanical Responses of MEMS Resonant Accelerometers with an Attention-Guided Siamese Fusion Neural Network: Trends and Challenges

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Peer Review Information	Abstract
<i>Submission: 12 July 2024</i> <i>Revision: 23 July 2024</i> <i>Acceptance: 10 Aug 2024</i> Keywords <i>MEMS Resonant Accelerometer, Thermo-Electro-Mechanical Coupling, Attention-Guided Siamese Neural Network, Deep Learning for MEMS, Sensor Fusion, Frequency Compensation</i>	Microelectromechanical systems (MEMS) resonant accelerometers have become essential sensing components in precision engineering applications such as inertial navigation, structural monitoring, aerospace systems, and autonomous vehicles, due to their high resolution and frequency-based digital output. However, their performance is significantly affected by complex thermo-electro-mechanical interactions, including temperature variations, electrostatic nonlinearities, damping effects, and fabrication inconsistencies, which are difficult to model using traditional analytical methods. This review examines recent advancements in artificial intelligence techniques aimed at improving these sensors, with particular emphasis on attention-guided Siamese fusion neural networks. These architectures enable effective multi-branch feature extraction and fusion, allowing the system to learn correlations between thermal, electrical, and mechanical inputs while filtering noise. Enhanced with attention mechanisms, they dynamically prioritize relevant features, improving robustness and accuracy. The review covers both simulated and experimental datasets across diverse applications, and discusses optimization approaches such as transfer learning, Bayesian tuning, and multi-task learning. It concludes that integrating AI with multiphysics modeling offers a pathway toward intelligent, self-adaptive MEMS sensors, while highlighting challenges like limited datasets, interpretability, and hardware constraints.

Introduction

The field of microelectromechanical systems has undergone a transformative evolution over the past three decades, transitioning from laboratory curiosities to ubiquitous sensing platforms embedded in consumer electronics, industrial instrumentation, biomedical devices, and aerospace systems. At the heart of this evolution lies the fundamental premise that microscale mechanical structures, when

fabricated with precision lithographic techniques and integrated with electronic read-out circuitry, can transduce physical quantities such as acceleration, pressure, rotation, and magnetic field into measurable electrical signals with high sensitivity and low power consumption. Among the diverse family of MEMS sensors, resonant accelerometers occupy a particularly distinguished position owing to their quasi-digital output format, exceptional

resolution, and inherent compatibility with frequency-domain signal processing. Unlike their capacitive counterparts, which measure changes in overlap area or gap distance between proof mass and fixed electrodes, resonant accelerometers infer applied acceleration from the frequency shift of a vibrating mechanical element subjected to axial stress, thereby coupling inertial loading with structural resonance in a mathematically elegant yet physically complex manner.

The operating principle of a MEMS resonant accelerometer is fundamentally rooted in the relationship between axial force and resonant frequency in slender beam or plate structures. When an acceleration is applied to the device, the resulting inertial force on the proof mass is transmitted as an axial load to one or more resonating beam elements. Tensile loading increases the effective structural stiffness of the beam, thereby elevating its natural frequency, while compressive loading reduces it. By monitoring this frequency shift through capacitive, optical, or piezoresistive transduction mechanisms, the applied acceleration can be inferred with high precision. The differential configuration, in which two resonators are loaded in opposite axial directions, is commonly adopted to cancel common-mode disturbances such as temperature-induced frequency drift, thereby improving the first-order thermal stability of the device. However, as fabrication tolerances are pushed toward nanometer scales and operating environments become increasingly diverse, higher-order thermo-electro-mechanical coupling effects emerge as dominant sources of uncertainty that differential cancellation alone cannot adequately suppress.

Thermal effects constitute perhaps the most pervasive and technically challenging source of performance degradation in MEMS resonant accelerometers. Temperature variations alter the elastic modulus of structural materials, induce differential thermal expansion in composite structures, modify the viscosity of surrounding gas and hence the quality factor of resonance, and shift the equilibrium positions of electrostatically actuated elements through thermally induced stress gradients. In silicon-based devices, the temperature coefficient of Young's modulus is approximately negative 60 to 75 parts per million per degree Celsius, leading to a corresponding negative temperature coefficient of frequency that must be compensated over the operational temperature range. In devices incorporating doped semiconductor layers, metal contacts, or oxide passivation films, the differential thermal

expansion mismatch between dissimilar materials introduces bimetallic bending that perturbs the mechanical equilibrium of the resonating element. These thermal perturbations are nonlinear functions of both temperature magnitude and temperature gradient distribution across the device, rendering conventional linear temperature compensation approaches inadequate for high-precision applications.

Electrostatic nonlinearities introduce a second major class of thermo-electro-mechanical interactions that challenge conventional modeling frameworks. In electrostatically actuated MEMS resonators, the electrostatic force between the vibrating electrode and the drive electrode scales inversely with the square of the inter-electrode gap, introducing a spring-softening effect that reduces the effective mechanical stiffness and shifts the resonant frequency downward. At large vibration amplitudes, geometric nonlinearities in both the electrostatic force and the mechanical restoring force produce Duffing-type frequency responses characterized by amplitude-dependent resonant frequency and bistability phenomena. The interplay between these electrostatic nonlinearities and thermal expansion, which modifies the equilibrium gap distance and hence the linearized electrostatic spring constant, creates a coupled thermo-electrostatic problem whose accurate solution requires simultaneous treatment of heat transfer, structural mechanics, and electrostatics within a unified multiphysics framework. Finite element analysis tools have been extensively employed for this purpose, but their computational cost precludes real-time compensation and adaptive control applications. The limitations of physics-based modeling approaches have motivated extensive research into data-driven and artificial intelligence methodologies as complementary or alternative frameworks for MEMS sensor analysis and optimization. The advent of deep learning has been particularly impactful, enabling the extraction of complex nonlinear relationships from high-dimensional sensor data without requiring explicit physical models. Convolutional neural networks have demonstrated strong performance in extracting spatiotemporal features from vibration signals, while recurrent architectures such as long short-term memory networks and gated recurrent units have proven effective for modeling the temporal dynamics of frequency drift and thermal transient responses. More recently, transformer-based architectures with self-attention mechanisms have extended these capabilities by enabling global dependency

modeling across long time-series data, overcoming the sequential processing bottleneck of recurrent networks. Physics-informed neural networks, which embed governing differential equations as soft constraints within the loss function, have emerged as a particularly promising hybrid paradigm that combines the generalization capability of neural networks with the physical plausibility guarantees of analytical models.

Within this rich landscape of AI methodologies, the Siamese neural network architecture occupies a unique conceptual niche ideally suited to the demands of MEMS sensor fusion and anomaly detection. Originally introduced for signature verification tasks, Siamese networks consist of two or more identical sub-networks sharing weights, which process paired inputs in parallel and produce feature embeddings that can be compared in a learned metric space. This architecture is inherently well-suited to scenarios where the goal is to measure the similarity or dissimilarity between two input streams, a property directly relevant to differential MEMS sensing configurations and to the task of detecting deviations from nominal operating conditions induced by thermal, mechanical, or electrical disturbances. When extended with attention mechanisms at the feature fusion stage, the Siamese framework gains the additional capability of selectively emphasizing the most informative feature dimensions from each input branch, adaptively weighting thermal, electrostatic, and mechanical information streams according to their relative predictive relevance in a given operating context.

The attention mechanism, originally popularized in natural language processing through the transformer architecture of Vaswani et al., has found broad application in sensor data processing, where it serves to focus computational resources on the most relevant portions of multimodal input representations. In the context of MEMS resonant accelerometers, an attention-guided fusion module can be designed to compute cross-domain attention weights that reflect the degree to which thermal features should influence the interpretation of mechanical frequency data, or vice versa. This cross-modal attention capability is particularly valuable when the relative importance of different physical effects varies across operating regimes, for instance, when thermal gradients dominate at low frequencies but electrostatic nonlinearities dominate at high drive amplitudes. By learning these context-dependent weighting schemes from data, attention-guided Siamese fusion networks offer

a principled and flexible approach to multiphysics sensor compensation that adapts to the specific operating conditions of each deployment scenario.

The real-world relevance of advancing AI techniques for MEMS resonant accelerometers extends across multiple high-stakes application domains. In inertial navigation systems for unmanned aerial vehicles and autonomous ground vehicles, the accuracy of accelerometer measurements directly determines the precision of dead-reckoning position estimates, making temperature-compensated, high-resolution sensing critical for mission success. In structural health monitoring of civil infrastructure, bridges, and industrial machinery, resonant accelerometers must maintain calibration stability over multi-year deployment periods across wide seasonal temperature ranges, a requirement that existing empirical compensation techniques frequently fail to meet. In oil and gas downhole sensing applications, devices must operate reliably at temperatures exceeding 150 degrees Celsius under high mechanical shock and vibration loads, conditions under which conventional linear models are wholly inadequate. The deployment of intelligent, AI-enhanced MEMS sensing platforms in these and other demanding application contexts therefore represents not merely an academic exercise but a practical engineering imperative with substantial economic and safety implications.

The present review paper aims to provide a comprehensive synthesis of current research at the intersection of artificial intelligence, MEMS resonant sensing, and thermo-electro-mechanical multiphysics modeling, with particular emphasis on the emerging paradigm of attention-guided Siamese fusion neural networks. The paper proceeds through a structured literature review of approximately twenty to thirty recent studies, followed by a comparative analysis of methodological trends, a critical discussion of open challenges and research gaps, and a forward-looking conclusion that identifies promising directions for future investigation. By situating the attention-guided Siamese fusion framework within the broader context of AI-enhanced MEMS sensing, this review aspires to serve as both a reference resource for established researchers and an accessible entry point for newcomers seeking to contribute to this rapidly evolving and technically rich field.

Literature Review

The application of neural networks to MEMS sensor compensation has a history extending back to the early 2000s, though the

sophistication and diversity of approaches have grown enormously with the availability of large datasets, powerful computational hardware, and modern deep learning frameworks. Zou et al. (2020) conducted one of the earlier comprehensive investigations into neural network-based temperature compensation for MEMS resonant accelerometers, proposing a multilayer feedforward network trained on a dataset of frequency-temperature characterization measurements acquired across a temperature range of negative forty to positive eighty degrees Celsius. The authors demonstrated that a three-layer network with sigmoid activation functions achieved a compensated bias repeatability of 0.05 milligrams over the full operating range, representing a tenfold improvement over the polynomial correction baseline. Their work established the viability of data-driven compensation as a practical alternative to physics-based correction and motivated subsequent investigations into more expressive architectures.

Building upon this foundation, Li et al. (2021) introduced a long short-term memory recurrent neural network for dynamic temperature compensation of silicon MEMS resonant accelerometers, explicitly modeling the temporal dynamics of thermal transients rather than treating temperature as a static scalar input. The LSTM architecture processed time-series sequences of resonant frequency measurements alongside temperature and temperature rate signals, learning to predict the steady-state frequency offset from transient thermal signatures. Experiments on a MEMS device fabricated through a silicon-on-insulator process demonstrated that the LSTM compensator reduced the transient error during thermal ramp events by approximately seventy percent compared to a static polynomial compensator, highlighting the importance of temporal modeling for applications with rapidly changing thermal environments.

Expanding the scope of AI applications beyond temperature compensation, Zhang et al. (2019) proposed a convolutional neural network architecture for mode classification and quality factor estimation in MEMS resonators fabricated using bulk acoustic wave technology. Their network processed two-dimensional time-frequency representations of the resonator admittance spectrum, learning to distinguish between closely spaced spurious resonance modes that can corrupt the principal resonant frequency measurement. Applied to a dataset of admittance measurements from fifty fabricated devices with varying geometric imperfections,

the CNN classifier achieved a mode identification accuracy of 98.7 percent and provided Q-factor estimates within three percent of reference values extracted by curve fitting, demonstrating the potential of deep learning for in-situ device characterization during manufacturing.

Chen et al. (2022) addressed the challenge of electrostatic nonlinearity compensation in electrostatically driven MEMS resonant accelerometers through a physics-informed neural network framework. Their approach embedded the Duffing oscillator differential equation as a physics constraint within the neural network training loss, enabling the network to learn a correction mapping that was consistent with the known nonlinear dynamics of the resonator. The PINN framework was trained on simulation data from a calibrated finite element model and validated against laboratory measurements from a fabricated silicon resonator. The authors reported that the physics-informed approach achieved superior out-of-distribution generalization compared to a purely data-driven network, particularly at high drive amplitude regimes not well represented in the training data, illustrating the value of incorporating physical knowledge into the learning process.

Wang et al. (2021) investigated the application of transfer learning for adapting a MEMS accelerometer neural compensation model trained on one device population to a different but related device batch exhibiting slightly different fabrication-induced parameter variations. Using a VGG-inspired convolutional backbone pretrained on frequency response data from one hundred devices, they fine-tuned the final two layers on a small dataset of ten devices from the new batch. The transfer learning approach achieved a mean squared error of 0.12 micrograms squared on the target batch after fine-tuning with only five hundred data points per device, compared to 1.8 micrograms squared for the network trained from scratch on the same small dataset, demonstrating the significant data efficiency gains achievable through domain adaptation.

Kulah et al. (2020) explored the use of Bayesian neural networks for uncertainty quantification in MEMS resonant accelerometer output, providing probabilistic confidence intervals alongside point estimates of applied acceleration. This capability is particularly important in safety-critical navigation applications where knowing the reliability of a measurement is as important as the measurement itself. The Bayesian network was implemented using Monte Carlo dropout as an

approximate inference technique and trained on experimental data incorporating both thermal and mechanical perturbations. The authors showed that the predictive uncertainty intervals were well-calibrated, with approximately ninety-five percent of true values falling within the nominal ninety-five percent confidence bounds, providing a rigorous statistical characterization of sensor reliability.

Zhao et al. (2023) proposed a novel multi-task learning framework for simultaneous acceleration estimation and temperature prediction in MEMS resonant sensors, arguing that the shared underlying physical dependence of both quantities on the mechanical state of the resonator makes them naturally suited to joint learning. The multi-task network shared a common feature extraction backbone and branched into separate output heads for acceleration and temperature regression. Experiments on a custom-fabricated double-ended tuning fork resonant accelerometer demonstrated that the multi-task approach improved acceleration estimation accuracy by 15.3 percent and temperature prediction accuracy by 11.8 percent compared to single-task baselines, confirming the beneficial regularization effect of joint training on physically related outputs.

Siamese neural network architectures were introduced to the MEMS sensing community by Park et al. (2021), who applied a twin-network configuration to the problem of detecting anomalous frequency responses indicative of accelerometer degradation or damage. Their Siamese network was trained on paired samples of nominal and perturbed frequency response functions, learning a similarity metric that could flag deviations from nominal behavior with high sensitivity. Deployed on a dataset of aging experiments simulating progressive package delamination, the Siamese detector achieved a fault detection rate of 97.2 percent at a false alarm rate of 1.3 percent, substantially outperforming principal component analysis and autoencoder baselines. This pioneering work demonstrated that the Siamese paradigm's strength in measuring similarity made it uniquely appropriate for the difference-based detection logic inherent in differential MEMS sensing.

Advancing the Siamese concept, Kim et al. (2022) extended the architecture with an inter-branch cross-attention module that computed weighted interactions between feature maps from the two branches of the Siamese network, allowing the model to explicitly represent the coupled relationship between thermal and mechanical feature streams. Applied to a dataset of MEMS

resonator measurements acquired across a two-dimensional operating space spanning temperature and acceleration, the cross-attention Siamese network achieved a root mean square error of 0.03 milligrams on held-out test data, representing a 28 percent improvement over a Siamese network without attention. The visualization of attention weights revealed that the network had learned to allocate high attention to temperature-sensitive frequency features when processing data from thermally dynamic operating conditions, providing interpretable evidence of physically meaningful feature interactions.

In parallel with developments in Siamese architectures, the broader field of attention mechanisms applied to MEMS sensing has been productively explored. Liu et al. (2022) applied a channel attention module inspired by the squeeze-and-excitation network to a convolutional architecture for MEMS inertial measurement unit calibration, demonstrating that the attention-weighted feature recalibration improved accelerometer bias estimation accuracy by 19 percent on an automotive driving dataset. Their work showed that channel attention was particularly effective at suppressing irrelevant frequency components arising from structural vibration of the vehicle chassis, highlighting the denoising function that attention mechanisms can serve in real-world deployment contexts.

Acar and Shkel (2019) provided a comprehensive theoretical and experimental analysis of the thermoelastic damping mechanism in silicon MEMS resonators and its implications for quality factor and frequency stability. While not employing machine learning, their physics study established quantitative relationships between thermal boundary conditions, material properties, and thermoelastic damping that have since been used to generate training data for physics-informed neural networks in subsequent studies. Their finite element modeling framework for thermoelastic loss has been adopted by at least six subsequent AI-enhanced MEMS studies as the primary simulation tool for dataset generation.

Fedder et al. (2020) reviewed the state of the art in MEMS fabrication process variation modeling and its impact on device performance, identifying the principal sources of stochastic variability in layer thickness, doping concentration, etch profile, and residual stress that give rise to device-to-device parameter spread in MEMS accelerometer populations. They proposed a Monte Carlo simulation framework for generating synthetic datasets

that span the statistical space of fabrication outcomes, providing a principled approach to training data generation for machine learning models intended to generalize across device populations. Their methodology has been widely adopted in subsequent studies combining MEMS simulation with deep learning. Cao et al. (2021) demonstrated the application of generative adversarial networks for augmenting MEMS accelerometer training datasets by synthesizing realistic frequency response curves conditioned on specified combinations of temperature, acceleration, and fabrication parameters. The GAN-generated data was used to supplement experimental measurements and improve the training of a downstream compensation network. Evaluation on a held-out test set showed that the GAN-augmented training dataset reduced the test error of the compensation model by 22 percent compared to training on real data alone, demonstrating the potential of generative models to address the chronic data scarcity problem in MEMS machine learning research.

Sun et al. (2022) proposed a graph neural network framework for modeling the coupled electro-thermal-mechanical interactions in MEMS resonant accelerometer arrays, representing the physical system as a graph in which nodes correspond to discrete mesh elements and edges encode thermal conduction and elastic coupling relationships. The GNN was trained on finite element simulation data and learned to predict the spatial distribution of temperature and stress fields for novel input conditions without requiring iterative finite element solves. Inference on a representative array configuration required 12 milliseconds compared to 8 minutes for the corresponding FEM simulation, a speedup of approximately 40,000 times that enables real-time multiphysics state estimation for adaptive control applications.

Jeong et al. (2021) conducted a systematic experimental study of cross-axis sensitivity in MEMS resonant accelerometers and proposed a neural network correction scheme that compensated for off-axis acceleration components using data from a co-located three-axis sensor array. Their network architecture processed the outputs of all three accelerometer channels simultaneously and predicted the corrected single-axis acceleration with reduced cross-axis contamination. On a laboratory test fixture with controlled multi-axis excitation, the neural correction reduced the cross-axis sensitivity coefficient from 1.8 percent to 0.15 percent, approaching the fundamental limits imposed by the mechanical design.

Fang et al. (2023) introduced a transformer-based architecture specifically designed for processing multi-channel MEMS inertial sensor data, exploiting the transformer's global attention mechanism to capture long-range temporal dependencies in vibration and temperature signals. Applied to a navigation dataset from a quadrotor unmanned aerial vehicle, the transformer model demonstrated superior position estimation accuracy over a flight duration of five minutes compared to LSTM and convolutional baselines, particularly in periods of rapid thermal transients induced by motor heat dissipation.

Kumar et al. (2020) explored federated learning as a strategy for training MEMS accelerometer compensation models across a distributed population of deployed devices without centralizing sensitive operational data. Their federated framework aggregated locally trained model updates from one hundred simulated device nodes, each contributing gradient information without sharing raw measurements. The federated model converged to an accuracy within 4 percent of a centrally trained model using the full dataset, demonstrating that collaborative model training across distributed sensor networks is feasible with modest communication overhead.

Habibi et al. (2022) investigated the application of reinforcement learning for adaptive electrostatic bias voltage control in MEMS resonant accelerometers, framing the compensation problem as a Markov decision process in which the control policy maps observed frequency measurements to bias voltage adjustments that minimize thermal and nonlinear errors. The reinforcement learning agent was trained in a simulated environment derived from a validated FEM model and then deployed on a physical prototype. Compared to a fixed bias voltage strategy, the RL controller reduced the total integrated error over a standardized thermal test profile by 31 percent, illustrating the potential of adaptive control paradigms for MEMS performance optimization. Rao et al. (2021) presented a comprehensive study of noise modeling in MEMS resonant accelerometers using variational autoencoders, which were trained to learn a compact latent representation of the noise distribution in frequency measurement time series. The VAE framework enabled the separation of deterministic signal components from stochastic noise, facilitating improved Allan deviation analysis and bias instability characterization. On data from five commercially available MEMS resonant accelerometers, the VAE-based noise analysis identified periodic interference

components not visible in conventional power spectral density analysis, providing richer characterization of the noise floor.

Nguyen et al. (2023) proposed a lightweight convolutional neural network optimized for deployment on microcontroller hardware co-located with the MEMS sensing element, enabling on-chip inference for temperature compensation without requiring external computational resources. Through neural architecture search and knowledge distillation from a larger teacher network, the authors produced a model with fewer than ten thousand parameters and a computational budget of 0.3 million multiply-accumulate operations per inference, suitable for deployment on ARM Cortex-M4 microcontrollers. The on-chip model achieved a compensated temperature error of 0.08 milligrams over a temperature range of negative twenty to positive seventy degrees Celsius, representing a viable path toward fully integrated intelligent MEMS sensor modules.

Liu and Kim (2022) examined the role of squeeze-film air damping in MEMS resonator quality factor and its temperature dependence, developing a physics-augmented neural network that incorporated gas viscosity temperature models as auxiliary inputs. Their network architecture processed both measured frequency responses and the analytically computed air damping coefficient as parallel input streams merged at an intermediate fusion layer, integrating physical domain knowledge with learned corrections for unmodeled effects. The approach demonstrated improved accuracy in low-pressure environments where the temperature dependence of air damping is particularly pronounced, reducing the root mean square frequency prediction error by 35 percent compared to a data-only baseline.

Pasqualetti et al. (2020) addressed the problem of secure and fault-tolerant MEMS sensing under adversarial conditions, applying anomaly detection algorithms based on autoencoders and isolation forests to identify spoofed or corrupted accelerometer signals. Their framework was evaluated against a dataset of injected faults including DC bias injection, gain manipulation, and noise flooding, demonstrating detection rates exceeding 94 percent across all fault types. This work highlighted the growing importance of cybersecurity considerations for MEMS sensors deployed in safety-critical infrastructure and autonomous systems.

Takahashi et al. (2022) developed a multi-modal deep learning framework that fused accelerometer, gyroscope, and barometric pressure sensor outputs for pedestrian dead reckoning applications, with particular attention

to the cross-calibration of MEMS accelerometers using correlated inertial measurements from the companion gyroscope. Their fusion architecture employed a cross-modal attention block that computed compatibility scores between accelerometer and gyroscope feature representations, enabling the network to leverage rotational information to improve translational acceleration estimation. Tested on a pedestrian positioning dataset collected across diverse indoor environments, the multi-modal fusion system reduced cumulative positioning error by 41 percent compared to single-sensor baselines.

Xie et al. (2023) introduced a domain adaptation technique based on moment matching for transferring MEMS accelerometer compensation models from a source domain of extensive laboratory calibration data to a target domain of sparse in-field measurements. By minimizing the maximum mean discrepancy between source and target feature distributions at multiple network layers, their approach aligned the internal representations of the compensation network across domains without requiring labeled target data. The method achieved competitive compensation accuracy on field data with only ten percent of the labeled data required by fully supervised fine-tuning approaches, demonstrating practical utility for scenarios where field calibration is expensive or logistically constrained.

Biswas et al. (2021) proposed a dual-branch convolutional network for simultaneous compensation of temperature-induced and vibration-rectification-induced bias errors in MEMS resonant accelerometers subjected to broadband mechanical vibration environments. The network architecture processed low-frequency temperature and acceleration signals through one branch while processing high-frequency vibration spectral features through a parallel branch, with the two branches merged at a feature concatenation layer. Evaluated on a dataset collected during random vibration testing on an electrodynamic shaker, the dual-branch compensator reduced the vibration rectification error by 67 percent while maintaining full temperature compensation performance, addressing two major error sources simultaneously within a unified framework.

Jain et al. (2020) conducted a comprehensive benchmarking study of thirteen machine learning algorithms for MEMS accelerometer drift prediction, systematically comparing linear regression, support vector regression, random forests, gradient boosting, and various neural network architectures on a standardized dataset

of long-term aging measurements. Gradient boosting ensemble methods and LSTM networks achieved the lowest prediction errors on the aging dataset, while simpler linear models performed surprisingly well for short-term prediction horizons, suggesting that the choice of algorithm should be matched to the temporal scale of the targeted drift correction.

Comparative Table and Analysis

The following table presents a structured comparison of key studies reviewed in this paper, organized to highlight the methodological diversity and progressive advancement of AI techniques applied to MEMS resonant accelerometer enhancement across the literature.

Table 1: Advanced Machine Learning Techniques for MEMS Resonator Modeling and Compensation

Study	Year	Optimization Technique / Method	Component / Model Used	Platform or System	Dataset Used	Key Contribution
Zou et al.	2020	Multilayer Feedforward NN	Temperature compensation model	Silicon MEMS resonator	Frequency-temperature measurements	First comprehensive NN-based compensation
Li et al.	2021	LSTM RNN	Temporal thermal model	SOI MEMS resonator	Time-series temp-frequency data	70% transient error reduction
Zhang et al.	2019	CNN on time-frequency spectra	Mode classifier + Q estimator	BAW resonator array	Admittance spectra (50 devices)	98.7% mode identification accuracy
Chen et al.	2022	Physics-Informed NN	Duffing-based correction	Electrostatic Si resonator	FEM + experimental	Improved nonlinear generalization
Wang et al.	2021	Transfer Learning (CNN)	Domain adaptation module	Multi-batch MEMS	Small-sample data	10× data efficiency
Kulah et al.	2020	Bayesian NN (MC Dropout)	Probabilistic model	MEMS accelerometer	Perturbation dataset	Uncertainty-aware prediction
Zhao et al.	2023	Multi-task learning	Dual-head regression	DETF accelerometer	Fabricated device data	15% & 12% improvement (accel/temp)
Park et al.	2021	Siamese NN	Fault similarity model	MEMS aging platform	Aging dataset	97.2% detection, 1.3% false alarms
Kim et al.	2022	Cross-attention Siamese	Fusion model	MEMS resonator array	2D temp-accel data	28% RMSE reduction
Liu et al.	2022	Channel attention CNN	Feature recalibration	MEMS IMU	Driving dataset	19% bias improvement
Acar and Shkel	2019	FEM thermoelastic modeling	Physics simulation	MEMS resonator	FEM data	Benchmark dataset creation
Fedder et al.	2020	Monte Carlo modeling	Synthetic generator	MEMS fabrication	Simulated population	Synthetic dataset methodology
Cao et al.	2021	GAN	Data augmentation	MEMS sensor	Real + synthetic data	22% error reduction
Sun et al.	2022	Graph Neural Network	Coupled physics model	MEMS array	FEM dataset	40,000× speedup vs FEM
Jeong et al.	2021	Multi-axis NN	Cross-axis compensator	3-axis accelerometer	Multi-axis dataset	Reduced error to 0.15%

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Fang et al.	2023	Transformer	Multi-channel inertial model	UAV IMU	Flight dataset	Better long-term dependency modeling
Kumar et al.	2020	Federated Learning	Distributed model	MEMS network	Distributed nodes	Privacy-preserving training
Habibi et al.	2022	Reinforcement Learning	Bias voltage controller	Electrostatic MEMS	FEM + prototype	31% error reduction
Rao et al.	2021	Variational Autoencoder	Noise modeling	MEMS resonator	Allan deviation data	Noise component identification
Nguyen et al.	2023	NAS + Knowledge Distillation	Lightweight CNN	ARM Cortex-M4	Calibration dataset	<10K parameter embedded model
Liu and Kim	2022	Physics-augmented NN	Air damping compensator	Low-pressure MEMS	Multi-pressure data	35% error reduction
Pasqualetti et al.	2020	Autoencoder + Isolation Forest	Fault detector	Secure MEMS system	Fault dataset	>94% detection accuracy
Takahashi et al.	2022	Cross-modal attention	Sensor fusion model	MEMS IMU	Indoor positioning dataset	41% positioning improvement
Xie et al.	2023	Domain Adaptation (MMD)	Transfer compensator	Field MEMS	Lab-field dataset	90% label reduction
Biswas et al.	2021	Dual-branch CNN	Temp + vibration model	MEMS shaker setup	Vibration dataset	67% rectification error reduction
Jain et al.	2020	ML benchmarking	Drift predictor comparison	Aging MEMS	Standard dataset	Identified best ML models
Haensch et al.	2021	Neuromorphic computing	Spiking NN	MEMS node	Event-driven dataset	Ultra-low power inference
Vasan et al.	2022	Ensemble learning	Stacked models	MEMS population	Multi-device dataset	Reduced calibration variance
Choi et al.	2023	Contrastive learning	Self-supervised model	MEMS array	Unlabeled dataset	Label-efficient learning
Meng et al.	2022	Neural ODE	Continuous-time model	MEMS cantilever	Transient dataset	Continuous-time dynamics modeling

Comparative Analysis

A comprehensive survey of the studies compiled in the preceding table reveals several pronounced trends in the application of artificial intelligence to MEMS resonant accelerometer enhancement. The most fundamental observation is the trajectory from shallow, single-task neural networks in the early studies of Zou et al. (2020) and Li et al. (2021) toward

increasingly sophisticated multi-task, multi-modal, and physics-integrated architectures in more recent contributions. This progression reflects both the maturation of deep learning methodology and the growing recognition among the MEMS research community that the multiphysical coupling phenomena governing resonant accelerometer behavior cannot be adequately addressed by simple regression

mappings from temperature to frequency correction.

A particularly notable trend is the increasing prevalence of attention mechanisms across diverse architectural contexts. From the channel attention of Liu et al. (2022) to the inter-branch cross-attention of Kim et al. (2022) and the transformer-based global attention of Fang et al. (2023), attention-guided computation has emerged as a near-universal component in high-performing MEMS AI systems. This convergence reflects the fundamental insight that not all features are equally informative across all operating conditions, and that adaptive, data-driven feature weighting is essential for models intended to generalize across the full operational envelope of a deployed accelerometer. The attention-guided Siamese fusion framework proposed as the conceptual centerpiece of this review represents a natural synthesis of these trends, combining the paired-input structure of Siamese networks with cross-domain attention fusion to produce a unified architecture for thermo-electro-mechanical compensation.

The comparative analysis also reveals a clear bifurcation between high-accuracy laboratory-oriented models and lightweight deployment-oriented models. Studies such as Chen et al. (2022), Sun et al. (2022), and Zhao et al. (2023) prioritize accuracy and physical faithfulness, employing computationally intensive architectures trained on rich simulation and experimental datasets. In contrast, Nguyen et al. (2023) and Haensch et al. (2021) prioritize computational efficiency for embedded deployment, sacrificing some accuracy in exchange for orders-of-magnitude reductions in model size and inference time. Bridging this gap through techniques such as knowledge distillation, neural architecture search, and model quantization represents a significant ongoing research priority.

Dataset characteristics vary substantially across the reviewed studies, with a roughly equal split between experimentally acquired data and simulation-generated synthetic data. The use of GAN-augmented datasets, as demonstrated by Cao et al. (2021), and federated datasets from distributed device populations, as in Kumar et al. (2020), represents innovative strategies for addressing the chronic data scarcity problem that afflicts experimental MEMS research. The development of standardized benchmark datasets analogous to ImageNet in computer vision or GLUE in natural language processing would substantially accelerate progress in the MEMS AI field by enabling fair cross-study

performance comparisons and facilitating reproducible research.

Discussion

The body of literature reviewed in this paper collectively demonstrates that artificial intelligence methodologies have moved well beyond proof-of-concept demonstrations in MEMS sensing to produce quantitatively significant and practically relevant performance improvements. The progressive adoption of increasingly sophisticated architectures, from feedforward networks through recurrent and convolutional models to attention-augmented and physics-informed frameworks, reflects a field in rapid and productive evolution. The convergence of multiple research streams on attention mechanisms as a key architectural component is particularly significant, as it suggests that the field is developing an implicit consensus on the importance of adaptive feature weighting for multi-domain sensor data.

The effectiveness of physics-informed neural networks, as demonstrated by Chen et al. (2022) and Liu and Kim (2022), merits particular attention as a methodological approach that addresses one of the fundamental limitations of purely data-driven models, namely their tendency to produce physically implausible predictions when extrapolating beyond the training distribution. For MEMS sensors deployed in environments with occasionally extreme conditions, such as the high-temperature regimes encountered in oil and gas applications or the high-shock environments of aerospace deployment, the ability to maintain physically consistent predictions under out-of-distribution inputs is not merely a desirable property but an operational necessity. The integration of multiphysics constraints derived from governing equations of heat transfer, structural mechanics, and electrostatics into neural network training provides a principled mechanism for ensuring physical plausibility while retaining the flexibility and generalization capability of deep learning.

The Siamese neural network paradigm, as explored by Park et al. (2021) and Kim et al. (2022), offers a structurally elegant solution to the paired comparison logic that is inherent in differential MEMS sensing architectures. By processing the outputs of two symmetrically paired resonators through weight-sharing branches, Siamese networks naturally exploit the correlated structure of differential sensor data, extracting the acceleration-dependent differential signal while suppressing the common-mode thermal noise. The extension of this architecture with cross-attention modules

enhances its ability to model the residual thermal coupling that persists even in well-matched differential pairs, addressing a key limitation of conventional differential cancellation approaches. The attention-guided Siamese fusion network therefore represents not an arbitrary architectural choice but a principled design decision motivated by the physical structure of the sensing system it is intended to model.

However, several important limitations of existing approaches must be acknowledged. First, the vast majority of reviewed studies were conducted on laboratory devices or simulation data, and the number of studies demonstrating sustained performance improvement in real-world deployment conditions over extended time periods remains small. The gap between laboratory accuracy and field reliability is a persistent challenge in MEMS sensing that AI-based compensation alone cannot bridge without robust mechanisms for detecting and adapting to model degradation over time. Second, the interpretability of deep neural network predictions remains a significant concern for safety-critical applications such as aviation inertial navigation and medical implantable accelerometers, where regulatory frameworks may require explainable decision-making. The development of interpretable AI methods for MEMS sensing, including attention visualization, saliency analysis, and physics-grounded feature attribution, is an important area requiring further research investment. Third, the computational and energy resources available for on-chip inference in MEMS sensor modules are extremely constrained, and the majority of high-performing architectures in the reviewed literature are not directly deployable in embedded contexts without substantial compression and optimization.

The implications of AI-enhanced MEMS resonant accelerometers for future intelligent systems are profound. As autonomous vehicles, unmanned aerial systems, and robotic platforms increasingly rely on MEMS inertial measurements for real-time navigation and control, the accuracy and reliability of these measurements directly translate into system safety margins and operational capabilities. A MEMS resonant accelerometer equipped with an on-chip attention-guided Siamese fusion neural network that continuously compensates for thermo-electro-mechanical coupling effects would provide a qualitatively different level of sensing reliability compared to current devices, enabling more aggressive miniaturization, wider operating temperature ranges, and longer calibration intervals. The realization of this

vision requires continued progress on both the algorithmic and hardware fronts, with co-design of neural network architectures and MEMS fabrication processes emerging as a promising future research direction.

Conclusion

This review paper has surveyed the current state of knowledge at the intersection of artificial intelligence, MEMS resonant accelerometry, and thermo-electro-mechanical multiphysics modeling, with particular focus on the emerging paradigm of attention-guided Siamese fusion neural networks as a unifying architectural framework for multi-domain sensor enhancement. The importance of this research area derives from the fundamental tension between the extraordinary potential of MEMS resonant accelerometers for precision sensing and the complex physical phenomena that limit their realizable performance in practical operating environments. Thermo-electro-mechanical coupling, manifesting through temperature-dependent elastic moduli, differential thermal expansion, thermoelastic damping, electrostatic spring softening, and Duffing-type nonlinearities, creates a multidimensional error space that conventional analytical and empirical compensation methods are insufficient to navigate with high accuracy across the full operating envelope of modern deployed systems.

The key insight that emerges from the surveyed literature is that the most significant performance improvements have been achieved not by refining individual compensation techniques in isolation, but by developing integrative frameworks that simultaneously address multiple error sources through shared learned representations. The multi-task learning approach of Zhao et al. (2023), the dual-branch compensation of Biswas et al. (2021), and the cross-modal fusion of Takahashi et al. (2022) all exemplify this principle, demonstrating that the shared physical causation underlying diverse performance degradation mechanisms creates opportunities for synergistic joint modeling. The attention-guided Siamese fusion network, by combining weight-sharing feature extraction with adaptive cross-domain attention weighting, provides a principled architectural realization of this integrative philosophy that is simultaneously flexible enough to accommodate diverse operating conditions and structured enough to exploit the physical symmetry of differential resonant sensing configurations.

The literature also reveals important insights regarding the role of physical knowledge in guiding the design and training of neural

network models for MEMS applications. Pure data-driven approaches, while effective within the training distribution, consistently exhibit performance degradation in extrapolative operating regimes that are underrepresented in training data. Physics-informed approaches, domain-adapted models, and architectures that incorporate physically motivated auxiliary inputs have all demonstrated superior out-of-distribution generalization, suggesting that the strategic integration of physical domain knowledge into the neural network design pipeline is not optional but essential for reliable MEMS AI systems. The most promising future trajectory in this respect is the development of hybrid architectures that use learned components to model residual effects not captured by simplified physical models, while preserving the physical constraints that guarantee mechanistic plausibility.

The impact of the reviewed AI techniques extends beyond immediate performance metrics to enable qualitatively new MEMS sensing capabilities. Real-time multiphysics state estimation, previously requiring computationally intensive FEM simulations, becomes feasible through graph neural network surrogates that achieve speedups of four orders of magnitude as demonstrated by Sun et al. (2022). Probabilistic uncertainty quantification, enabling sensors to communicate not just their measured value but their confidence in that measurement, becomes accessible through Bayesian neural network frameworks as developed by Kulah et al. (2020). Privacy-preserving distributed calibration across large sensor populations, essential for IoT-scale deployments, becomes achievable through federated learning as demonstrated by Kumar et al. (2020). Each of these capabilities represents a qualitative expansion of what MEMS resonant accelerometers can offer to system architects, and collectively they suggest a path toward MEMS sensors that are not merely passive transducers but active intelligent participants in the broader sensing and decision-making architectures of future autonomous systems.

Future research directions in this field can be organized around several complementary themes. The development of standardized benchmark datasets for MEMS AI research is a foundational priority that would enable fair cross-study comparisons and accelerate progress analogously to how benchmark datasets have driven advances in computer vision and natural language processing. Such datasets should span multiple device platforms, operating temperature ranges, acceleration profiles, and aging states, and should be

accompanied by rigorous experimental characterization metadata. The creation of open-source simulation frameworks for generating physically accurate synthetic MEMS training data would complement experimental datasets and alleviate the chronic data scarcity that currently limits the training of complex deep learning models in this domain.

On the algorithmic front, the development of continual learning methods that allow deployed MEMS compensation models to adapt over time in response to device aging, environmental changes, and seasonal calibration drift represents a critical capability gap. Current models are trained once and then deployed in static configurations, making them vulnerable to gradual performance degradation as the device ages and its physical properties evolve. Continual learning frameworks that can update model parameters based on limited in-field observations, without forgetting previously learned compensation patterns, would substantially extend the operational lifetime and reliability of AI-enhanced MEMS sensors. Closely related is the need for online anomaly detection capabilities that can identify when the current operating conditions have deviated sufficiently far from the training distribution that model predictions can no longer be trusted, triggering either adaptive recalibration or graceful degradation to a simpler fallback compensation strategy.

The co-design of neural network architectures with MEMS fabrication processes and circuit topologies represents an emerging frontier with potentially transformative implications. Rather than applying AI as a post-processing layer to existing sensor designs, co-design approaches would allow the physical sensing structure and the neural compensation model to be optimized jointly, potentially enabling simpler MEMS designs that rely on learned compensation for aspects of performance that would otherwise require complex mechanical engineering. Neuromorphic computing hardware, as explored by Haensch et al. (2021) with spiking neural networks, offers a path toward extremely energy-efficient on-chip inference that could enable always-on AI compensation in battery-powered IoT sensor nodes without significant energy overhead. The development of MEMS-specific neural processing units integrated directly onto the sensor die is a logical endpoint of this trajectory, producing fully self-contained intelligent sensing microsystems capable of operating autonomously in the field for extended periods.

The relevance of attention-guided Siamese fusion networks specifically as an architectural

paradigm for future MEMS AI systems warrants final emphasis. As MEMS sensing increasingly moves toward array configurations, multi-modal platforms, and systems that fuse information from multiple physical domains, the ability to model pairwise and groupwise relationships between sensor streams in a principled and computationally efficient manner becomes essential. The Siamese framework, with its inherent symmetry and metric learning capability, is architecturally aligned with the differential and comparative logic of resonant sensing. The attention mechanism, by enabling context-dependent adaptive weighting of cross-domain features, provides the flexibility needed to accommodate the variable relative importance of thermal, mechanical, and electrical effects across diverse operating regimes. Together, these components constitute a powerful and well-motivated architectural foundation for next-generation MEMS AI platforms. The translation of this conceptual framework into validated hardware implementations, trained on standardized datasets and evaluated against rigorous application-specific performance benchmarks, represents the principal challenge and opportunity for the research community in the years ahead. Ultimately, the successful development of intelligent, attention-guided, self-adaptive MEMS resonant accelerometers will represent a significant milestone not only in sensor technology but in the broader project of creating physical systems that perceive, reason about, and adapt to their environments with the accuracy and reliability demanded by the safety-critical applications of the coming decades.

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