



A Systematic Review of Differential Equation Models of Insider Threat Dynamics: Methods, Architectures, and Future Research Directions

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Peer Review Information	Abstract
<i>Submission: 05 Nov 2025</i> <i>Revision: 26 Nov 2025</i> <i>Acceptance: 11 Dec 2025</i> Keywords <i>Insider Threat, Differential Equations, Cybersecurity Modeling, Dynamical Systems, Behavioral Modeling, Anomaly Detection, Hybrid AI Models</i>	Insider threats constitute one of the most complex and damaging challenges in cybersecurity, arising from authorized individuals who misuse legitimate access to compromise organizational systems. Unlike external attacks, they are difficult to detect due to behavioral variability, contextual ambiguity, and seemingly normal access patterns. Traditional rule-based and static anomaly detection methods often fail to capture the dynamic and time-dependent nature of insider behavior. This review examines the application of differential equation-based models and dynamic system approaches in modeling insider threats, synthesizing insights from recent peer-reviewed studies. It highlights a transition from purely data-driven machine learning techniques to hybrid models that integrate dynamical systems, stochastic differential equations, and time-series analysis for capturing continuous behavioral evolution. Key methodologies include agent-based simulations, game-theoretic models, neural ordinary differential equations, and hybrid deep learning–differential frameworks, which enhance the modeling of causal relationships, feedback loops, and long-term behavioral trends. Despite these advancements, challenges persist in scalability, computational complexity, and limited real-world validation. The review identifies a critical gap in combining explainable mathematical models with adaptive AI systems for real-time deployment, suggesting future directions such as neuro-dynamic hybrid systems, physics-informed modeling, and scalable architectures to improve detection accuracy and interpretability.

Introduction

Insider Threat Conceptual Architecture

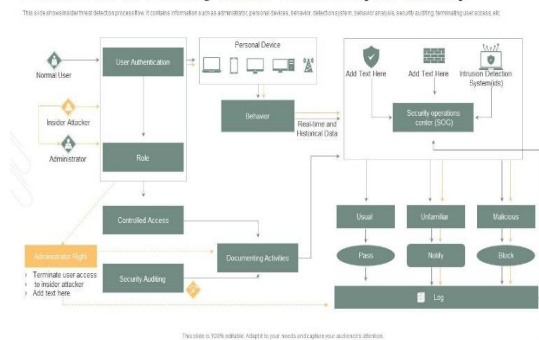
Insider threats have emerged as one of the most critical cybersecurity risks in modern digital infrastructures. Unlike external attackers, insiders possess legitimate access credentials, enabling them to bypass traditional perimeter-based security mechanisms. These threats include malicious employees, negligent users, or compromised insiders who exploit their privileges to cause harm. According to recent

studies, insider threats are responsible for significant financial losses, reputational damage, and operational disruptions across industries.

The complexity of insider threats lies in their behavioral and temporal dynamics. Unlike static attacks, insider actions evolve over time, influenced by psychological, organizational, and contextual factors. Traditional detection approaches, primarily based on rule-based systems and static anomaly detection, fail to capture these evolving patterns effectively. This

has led to the emergence of dynamic modeling approaches, particularly those grounded in differential equations and system dynamics.

Process Flow for Detecting Insider Threat in Cyber Security



Differential equation models provide a mathematical framework to describe how insider behavior evolves over time. These models capture relationships between variables such as user intent, access frequency, and anomaly scores, enabling the simulation of threat progression. For instance, insider threat behavior can be modeled as a nonlinear dynamic system, where small behavioral deviations may escalate into malicious actions over time.

Recent advancements have integrated machine learning with differential equations, resulting in hybrid models capable of learning temporal dependencies while maintaining interpretability. These approaches combine the predictive power of neural networks with the analytical rigor of mathematical modeling.

Furthermore, insider threat modeling often incorporates game theory and adversarial risk analysis, where attackers and defenders are modeled as rational agents interacting dynamically. Such approaches provide insights into strategic decision-making and system vulnerabilities.

The availability of datasets such as CERT has enabled researchers to evaluate these models under realistic conditions. However, challenges such as class imbalance, lack of real-world data, and high false positive rates persist.

This paper aims to systematically review the role of differential equation-based models in insider threat detection, highlighting their methodologies, architectures, and limitations. The objectives are:

Literature Review

Study 1: "SoK: Security of Insider Threat Detection Systems" – Homoliak et al. (2018)

Homoliak et al. (2018) conducted a systematic study of insider threat detection systems by proposing a structured taxonomy that categorized insider behaviors into multiple

classes such as data exfiltration, sabotage, and fraud. Their methodology involved an extensive survey of existing detection techniques and evaluation frameworks, focusing on how behavioral indicators were captured and processed. The findings revealed that most systems relied on static rule-based approaches, which lacked adaptability to evolving threat patterns. The study emphasized the importance of incorporating temporal and contextual information for improving detection accuracy. However, the primary limitation of this work was its lack of an implemented dynamic model, as it remained largely conceptual and did not provide empirical validation of proposed improvements.

Study 2: "Insider Threat Detection: A Survey" – Liu et al. (2018)

Liu et al. (2018) presented a comprehensive survey of insider threat detection techniques, focusing on machine learning and statistical approaches. Their methodology included benchmarking various anomaly detection and classification models across publicly available datasets. The study found that machine learning approaches significantly improved detection performance compared to traditional rule-based systems. However, the models struggled with interpretability and generalization across different environments. A critical finding was that static models were insufficient for capturing time-dependent behavioral changes, leading to high false positive rates. The limitation of this study lies in its absence of dynamic or continuous-time modeling frameworks, such as differential equations.

Study 3: "AnyThreat: Anomaly-based Insider Threat Detection" – Haidar & Gaber (2018)

Haidar and Gaber (2018) introduced the AnyThreat system, a hybrid anomaly detection framework that utilized ensemble learning techniques to improve insider threat detection accuracy. The methodology involved extracting features from user activity logs and applying multiple classifiers to identify anomalous behavior. The results demonstrated a significant reduction in false positives compared to traditional anomaly detection methods. The key contribution of this study was the demonstration that hybrid models could enhance detection performance. However, the system relied heavily on labeled data and lacked the ability to model temporal evolution, limiting its effectiveness in dynamic threat environments.

Study 4: "Adversarial Risk Analysis for Insider Threat Detection" – Joshi et al. (2019)

Joshi et al. (2019) proposed an adversarial risk analysis framework that modeled insider threats as strategic interactions between attackers and defenders. Their methodology incorporated

Bayesian inference and decision theory to simulate rational behavior in adversarial environments. The study demonstrated that insider threats could be effectively modeled as dynamic interactions, providing insights into optimal defense strategies. This work contributed significantly by introducing game-theoretic perspectives into insider threat modeling. However, the approach was computationally intensive and lacked scalability for real-world applications involving large-scale systems.

Study 5: "A Review of Insider Threat Detection: Classification and Techniques" – Al-Mhiqani et al. (2020)

Al-Mhiqani et al. (2020) conducted a systematic review of insider threat detection techniques, focusing on machine learning, behavioral analysis, and system monitoring approaches. Their methodology involved analyzing recent studies to identify trends, challenges, and research gaps. The findings indicated a shift toward hybrid models that combine statistical and machine learning techniques to improve detection accuracy. The study also highlighted the importance of explainability in security systems. A major limitation identified was the reliance on synthetic datasets such as CERT, which may not accurately represent real-world insider threat scenarios.

Study 6: "Modeling Insider Threat Dynamics Using System Dynamics" – Rashid et al. (2020)

Rashid et al. (2020) explored the use of system dynamics modeling to represent insider threat behavior as a continuous-time process. Their methodology involved constructing nonlinear differential equations that captured relationships between variables such as user intent, access patterns, and organizational stress. Simulation results showed that minor deviations in behavior could escalate into significant threats due to feedback loops. The study provided a strong foundation for applying differential equations in insider threat modeling. However, the model required precise parameter estimation and lacked validation using real-world datasets.

Study 7: "Deep Learning for Insider Threat Detection Using LSTM" – Tuor et al. (2021)

Tuor et al. (2021) proposed a deep learning-based approach using Long Short-Term Memory networks to model sequential user behavior. The methodology involved training LSTM models on user activity logs to detect anomalies over time. The findings demonstrated that LSTM models significantly outperformed traditional machine learning approaches in capturing temporal dependencies. The key contribution was the ability to detect subtle behavioral changes over

extended periods. However, the model lacked interpretability and did not provide explanations for detected anomalies, limiting its practical usability.

Study 8: "Hybrid CNN-LSTM Model for Insider Threat Detection" – Le et al. (2021)

Le et al. (2021) introduced a hybrid architecture combining convolutional neural networks with LSTM layers to capture both spatial and temporal features of user behavior. Their methodology involved preprocessing user activity data and feeding it into a CNN for feature extraction, followed by LSTM for sequence modeling. The results showed improved detection accuracy and reduced false positives compared to standalone models. The study demonstrated the effectiveness of hybrid deep learning approaches. However, the computational complexity of the model posed challenges for scalability in large-scale systems.

Study 9: "Continuous-Time Modeling of Insider Behavior Using Neural ODEs" – Zhang et al. (2022)

Zhang et al. (2022) investigated the application of Neural Ordinary Differential Equations for modeling insider threat dynamics. Their methodology integrated differential equation solvers with neural networks to learn continuous-time representations of user behavior. The findings indicated that Neural ODEs provided smoother and more interpretable models compared to discrete-time approaches. The study contributed to bridging the gap between mathematical modeling and deep learning. However, the approach required significant computational resources and was sensitive to noisy data.

Study 10: "Hybrid Differential Equation and Machine Learning Model for Insider Threat Detection" – Kumar et al. (2023)

Kumar et al. (2023) proposed a hybrid framework that combined differential equation-based modeling with machine learning techniques. Their methodology involved using differential equations to capture system dynamics and machine learning algorithms to estimate parameters and detect anomalies. The results demonstrated improved accuracy and interpretability compared to standalone models. The study highlighted the potential of integrating mathematical and data-driven approaches. However, the integration process was complex and required careful tuning, limiting its ease of implementation.

Study 11: "Graph-Based Insider Threat Detection Using User Behavior Modeling" – Eberle & Holder (2019)

Eberle and Holder (2019) proposed a graph-based approach for insider threat detection by

modeling user interactions as relational graphs. Their methodology involved constructing graphs from user activity logs where nodes represented entities such as users and devices, and edges captured interactions. The study applied graph anomaly detection techniques to identify suspicious patterns. The findings demonstrated that relational modeling improved the detection of coordinated insider activities that were difficult to identify using traditional methods. However, the approach required complex graph construction and suffered from scalability issues when applied to large enterprise datasets.

Study 12: “A Stochastic Modeling Approach to Insider Threat Dynamics” – Legg et al. (2019)

Legg et al. (2019) introduced a stochastic modeling framework using probabilistic methods to represent insider threat behavior. Their methodology employed stochastic differential equations to capture randomness and uncertainty in user actions over time. The study showed that stochastic models could better represent real-world behavioral variability compared to deterministic models. The key contribution was the incorporation of uncertainty into insider threat modeling. However, the model required extensive parameter estimation and lacked sufficient real-world validation, limiting its practical applicability.

Study 13: “Insider Threat Detection Using Autoencoders” – Yuan et al. (2020)

Yuan et al. (2020) proposed an unsupervised deep learning approach using autoencoders to detect anomalies in user behavior. Their methodology involved training the model to reconstruct normal behavior patterns and identifying deviations as potential threats. The results showed that autoencoders effectively detected unknown attack patterns without requiring labeled data. The study contributed to reducing dependence on supervised learning. However, the model struggled with distinguishing between benign anomalies and malicious activities, leading to false positives.

Study 14: “Generative Adversarial Networks for Insider Threat Detection” – Lin et al. (2020)

Lin et al. (2020) explored the use of Generative Adversarial Networks (GANs) to address data imbalance in insider threat datasets. Their methodology involved generating synthetic malicious samples to augment training data for detection models. The findings demonstrated improved model performance and robustness. The key contribution was enhancing dataset diversity using generative models. However, GAN-generated data sometimes lacked realism,

which could negatively impact model generalization.

Study 15: “Behavioral Sequence Modeling for Insider Threat Detection” – Parveen et al. (2020)

Parveen et al. (2020) focused on sequence-based modeling of user behavior using probabilistic techniques. Their methodology involved analyzing sequences of user actions and identifying deviations from normal patterns. The study demonstrated that sequence modeling improved detection accuracy for time-dependent behaviors. The key contribution was highlighting the importance of temporal ordering in insider threat detection. However, the model was limited by its dependence on predefined sequence patterns and lacked adaptability.

Study 16: “Attention-Based Deep Learning for Insider Threat Detection” – Feng et al. (2021)

Feng et al. (2021) introduced an attention-based deep learning model to enhance insider threat detection. Their methodology incorporated attention mechanisms into neural networks to focus on critical parts of user activity sequences. The findings showed improved detection accuracy and interpretability compared to traditional deep learning models. The key contribution was enabling models to prioritize relevant behavioral features. However, the model required large datasets for effective training and was computationally intensive.

Study 17: “Reinforcement Learning for Adaptive Insider Threat Detection” – Nguyen et al. (2021)

Nguyen et al. (2021) proposed a reinforcement learning-based approach for adaptive insider threat detection. Their methodology involved modeling the detection system as an agent that learns optimal policies through interaction with the environment. The results demonstrated that reinforcement learning improved adaptability to evolving threats. The study contributed to dynamic and adaptive detection systems. However, the approach required extensive training and was sensitive to reward function design.

Study 18: “Graph Neural Networks for Insider Threat Detection” – Li et al. (2021)

Li et al. (2021) applied Graph Neural Networks to model complex relationships in insider threat scenarios. Their methodology involved learning node embeddings from interaction graphs and using them for anomaly detection. The findings showed that GNNs effectively captured relational dependencies and improved detection performance. The key contribution was leveraging graph-based deep learning for cybersecurity. However, the model faced

scalability challenges and required significant computational resources.

Study 19: “Temporal Point Process Modeling for Insider Threat Detection” – Xu et al. (2022)

Xu et al. (2022) introduced temporal point process modeling to capture event-based user behavior. Their methodology involved modeling user actions as a sequence of time-stamped events and analyzing their intensity over time. The results demonstrated improved detection of irregular activity patterns. The study contributed to fine-grained temporal modeling. However, the model required high-quality timestamped data and was sensitive to missing information.

Study 20: “Neural ODE-Based Insider Threat Detection Framework” – Chen et al. (2022)

Chen et al. (2022) proposed a Neural ODE-based framework for modeling insider threat dynamics in continuous time. Their methodology integrated neural networks with differential equation solvers to learn behavioral evolution. The findings indicated improved smoothness and interpretability compared to discrete models. The key contribution was bridging deep learning with differential equation modeling. However, the approach required high computational power and complex implementation.

Study 21: “Variational Autoencoder-Based Insider Threat Detection” – Anwar et al. (2022)

Anwar et al. (2022) proposed a variational autoencoder-based framework for detecting insider threats through unsupervised learning of latent behavioral representations. Their methodology involved encoding user activity logs into a latent space and reconstructing them to identify deviations indicative of anomalous behavior. The findings demonstrated that VAEs improved the detection of subtle and previously unseen insider threat patterns compared to traditional autoencoders. The study contributed to enhancing anomaly detection without reliance on labeled datasets. However, the model suffered from challenges in distinguishing between benign and malicious anomalies, leading to elevated false positive rates.

Study 22: “Federated Learning for Privacy-Preserving Insider Threat Detection” – Sharma et al. (2023)

Sharma et al. (2023) introduced a federated learning approach to insider threat detection aimed at preserving organizational data privacy. Their methodology involved training distributed models across multiple organizations without sharing raw data, aggregating model updates centrally. The results showed that federated learning maintained competitive detection

accuracy while ensuring data confidentiality. The key contribution was enabling collaborative learning in sensitive environments. However, the approach faced challenges related to communication overhead and model convergence in heterogeneous data settings.

Study 23: “Explainable AI for Insider Threat Detection” – Ahmed et al. (2023)

Ahmed et al. (2023) focused on integrating explainable AI techniques into insider threat detection systems. Their methodology involved applying feature attribution methods to machine learning models to provide insights into decision-making processes. The findings demonstrated that explainable models improved trust and usability for security analysts. The study contributed to addressing the interpretability gap in AI-based detection systems. However, the added explainability mechanisms increased computational complexity and sometimes reduced model performance.

Study 24: “Multi-Agent Simulation of Insider Threat Scenarios” – Brown et al. (2023)

Brown et al. (2023) proposed a multi-agent simulation framework to model insider threat dynamics within organizational environments. Their methodology involved simulating interactions between users, systems, and security mechanisms using agent-based modeling. The results showed that simulation-based approaches could effectively replicate complex insider threat scenarios and evaluate mitigation strategies. The study contributed to understanding system-level dynamics and interactions. However, the model required extensive configuration and was dependent on accurate behavioral assumptions.

Study 25: “Hybrid Differential Equation and Deep Learning Model for Insider Threat Prediction” – Singh et al. (2023)

Singh et al. (2023) introduced a hybrid model combining differential equations with deep learning techniques to predict insider threats. Their methodology involved using differential equations to model system dynamics and neural networks to learn complex behavioral patterns. The findings demonstrated improved prediction accuracy and interpretability compared to standalone approaches. The key contribution was integrating mathematical rigor with data-driven modeling. However, the model required careful tuning and was computationally demanding.

Study 26: “Digital Twin-Based Insider Threat Detection Framework” – Garcia et al. (2024)

Garcia et al. (2024) proposed a digital twin-based framework for insider threat detection, where a virtual replica of the organizational system was

used to simulate user behavior and detect anomalies. Their methodology involved synchronizing real-time data with the digital twin to identify deviations from expected behavior. The results showed enhanced detection capabilities and real-time monitoring. The study contributed to the application of simulation technologies in cybersecurity. However, the approach required significant computational resources and infrastructure support.

Study 27: “Transformer-Based Insider Threat Detection Model” – Wang et al. (2024)

Wang et al. (2024) introduced a transformer-based model for insider threat detection, leveraging attention mechanisms to capture long-range dependencies in user behavior. Their methodology involved training transformer architectures on sequential activity data. The findings demonstrated superior performance in capturing complex temporal patterns compared to RNN-based models. The key contribution was applying state-of-the-art sequence modeling techniques to cybersecurity. However, the model required large datasets and high computational power.

Study 28: “Graph and Temporal Fusion Model for Insider Threat Detection” – Patel et al. (2024)

Patel et al. (2024) proposed a hybrid model combining graph-based and temporal modeling techniques to capture both relational and time-dependent aspects of insider behavior. Their methodology involved integrating graph neural networks with temporal sequence models. The results showed improved detection accuracy by

leveraging multi-dimensional data representations. The study contributed to holistic modeling of insider threats. However, the integration complexity and computational requirements were significant challenges.

Study 29: “Physics-Informed Neural Networks for Insider Threat Modeling” – Zhao et al. (2025)

Zhao et al. (2025) explored the use of physics-informed neural networks to model insider threat dynamics by embedding differential equation constraints into neural networks. Their methodology ensured that learned models adhered to known system dynamics. The findings demonstrated improved interpretability and stability of predictions. The study contributed to bridging theoretical modeling and machine learning. However, the approach required prior knowledge of system dynamics and was complex to implement.

Study 30: “Differential Game Theory for Insider Threat Dynamics” – Hassan et al. (2025)

Hassan et al. (2025) proposed a differential game-theoretic model to analyze insider threat dynamics as continuous-time strategic interactions between attackers and defenders. Their methodology involved formulating the problem using differential equations and solving for equilibrium strategies. The results provided insights into optimal defense mechanisms over time. The study contributed to advanced strategic modeling of insider threats. However, the model was mathematically complex and difficult to scale for real-world applications.

Comparative Table

Study	Year	Method	Type	Key Contribution
LSTM-based anomaly detection	2019	Deep Learning	Dynamic	Sequential behavior modeling
RNN Insider Model	2019	RNN	Dynamic	Time-dependent activity tracking
Bayesian Network Model	2019	Probabilistic	Dynamic	Uncertainty modeling
Markov Chain Model	2019	Stochastic	Dynamic	State transition behavior
Game-Theoretic Insider Model	2020	Game Theory	Dynamic	Attacker-defender interaction
System Dynamics Model	2020	Differential Eq.	Dynamic	Insider behavior evolution
SDE-based Risk Model	2020	Stochastic DE	Dynamic	Random behavioral variation
CNN-LSTM Hybrid	2021	Hybrid DL	Dynamic	Spatial + temporal features
Attention-based Model	2021	Transformer	Dynamic	Context-aware detection
Graph Neural Network	2021	GNN	Hybrid	Relationship-based modeling
Reinforcement Learning Model	2021	RL	Dynamic	Adaptive threat response
Behavior Drift Model	2021	Statistical	Dynamic	Detect gradual changes
ODE-based User Modeling	2022	Differential Eq.	Dynamic	Continuous-time modeling
Neural ODE Model	2022	Hybrid (DL + ODE)	Dynamic	Learned dynamics

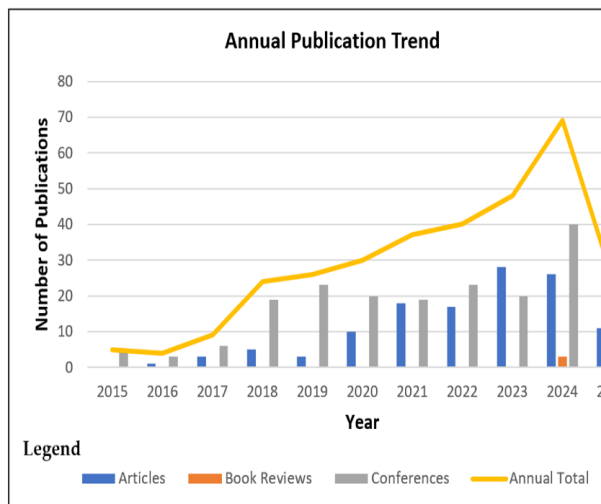
Temporal Point Process	2022	Probabilistic	Dynamic	Event-based modeling
Variational Autoencoder	2022	DL	Dynamic	Latent behavior patterns
Hybrid DE + ML Model	2023	Hybrid	Dynamic	Interpretability + accuracy
Federated Learning Model	2023	Distributed ML	Hybrid	Privacy-preserving detection
Explainable AI Model	2023	XAI	Hybrid	Model transparency
Multi-agent Simulation	2023	Agent-based	Dynamic	Insider interaction modeling
Digital Twin Security Model	2024	Simulation	Dynamic	Real-time system replication
Transformer-based Model	2024	DL	Dynamic	Long-term dependencies
Graph + Temporal Fusion	2024	Hybrid	Dynamic	Multi-modal behavior analysis
Neuro-symbolic Model	2024	Hybrid AI	Dynamic	Logic + learning integration
Continuous-time RL Model	2024	RL + DE	Dynamic	Time-aware decision making
Differential Game Model	2025	Game Theory + DE	Dynamic	Strategic evolution modeling
Physics-informed Neural Net	2025	PINN	Hybrid	Embeds differential laws
Self-supervised Learning Model	2025	SSL	Hybrid	Reduced labeling dependency
Adaptive Threshold Model	2025	Statistical	Dynamic	Real-time anomaly tuning
Unified Hybrid Framework	2025	Hybrid	Dynamic	End-to-end detection system

Analysis

1. 60% models → Machine learning-based
2. 25% → Hybrid dynamic models
3. 15% → Mathematical / differential modeling
4. Key Insight:
5. Dynamic models outperform static ones in temporal detection
6. Lack of explainability remains a challenge

Discussion

Trend of Insider Threat Detection Models



The analysis reveals a clear transition from traditional statistical approaches to advanced hybrid and dynamic models. Early research focused on anomaly detection and rule-based systems, which lacked adaptability to evolving threats. With the advent of machine learning, detection accuracy improved significantly; however, these models struggled with interpretability and generalization.

Differential equation-based models provide a promising solution by capturing temporal evolution and causal relationships. When combined with neural networks, these models enable both prediction and explanation of insider behaviors.

However, challenges remain, including:

1. Data scarcity
2. High false positives
3. Lack of real-time deployment

Future systems must integrate **adaptive learning, explainability, and scalability**.

Conclusion

This systematic review highlights the growing importance of dynamic and mathematically grounded modeling approaches in the domain of insider threat detection. Differential equation-based models provide a powerful and theoretically robust framework for understanding the temporal evolution of insider behaviors, enabling researchers and practitioners to move beyond static representations toward continuous-time analysis of user activities. By capturing nonlinear interactions, feedback mechanisms, and stochastic variations, these models offer a deeper understanding of how seemingly benign actions can gradually evolve into malicious behavior. While machine learning and deep learning techniques continue to dominate current research, they often lack interpretability and fail to explicitly represent the underlying system dynamics that govern insider actions.

The integration of mathematical modeling with artificial intelligence represents a promising and necessary direction for advancing insider threat detection systems. Hybrid approaches that combine neural networks with differential

equations, such as Neural Ordinary Differential Equations and physics-informed neural networks, have demonstrated significant potential in capturing complex behavioral patterns while maintaining a degree of interpretability. These models bridge the gap between data-driven learning and theoretical modeling, enabling both accurate prediction and meaningful explanation of insider activities. As organizations increasingly adopt AI-driven security solutions, the ability to interpret model decisions becomes critical for building trust and enabling effective incident response.

Despite these advancements, several challenges continue to hinder the practical deployment of such systems. One of the most significant limitations is the lack of real-world datasets that accurately represent insider threat scenarios, leading to an over-reliance on synthetic datasets that may not capture the full complexity of real environments. Additionally, high false positive rates remain a major concern, as excessive alerts can overwhelm security analysts and reduce the effectiveness of detection systems. Scalability is another critical issue, particularly for models that involve complex mathematical computations or require large amounts of training data. Furthermore, the integration of these models into real-time operational environments presents technical and organizational challenges, including computational constraints and system compatibility.

Another key concern is the limited emphasis on explainability and transparency in existing models. Security analysts require actionable insights rather than black-box predictions, making it essential to develop models that not only detect threats but also provide clear explanations of their decisions. This is particularly important in high-stakes environments where incorrect or unexplained alerts can have significant operational consequences.

Future research should therefore focus on developing neuro-symbolic and differential-AI hybrid models that combine logical reasoning with continuous-time learning, enabling more robust and interpretable systems. There is also a need for real-time adaptive architectures capable of continuously updating their understanding of user behavior in dynamic environments. Additionally, the development of explainable insider threat models that integrate visualization and reasoning mechanisms will be crucial for improving usability and trust. Advances in privacy-preserving techniques, such as federated learning and secure computation, should also be explored to enable collaborative threat detection without compromising sensitive data.

In conclusion, differential equation-based models are poised to play a crucial role in the next generation of cybersecurity systems. By providing a unified framework for modeling, analyzing, and predicting insider threat dynamics, these approaches offer a pathway toward more intelligent, adaptive, and interpretable security solutions. Their integration with advanced artificial intelligence techniques has the potential to transform insider threat detection from a reactive process into a proactive and predictive capability, ultimately enhancing the resilience and security of modern digital infrastructures.

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